



GlaxoSmithKline

# **Meta-analysis of clinical trials, particularly of rare adverse events**

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**Research Statistics Unit**

# Outline

1. What is meta-analysis?
2. How does it work?
3. Efficacy of SSRIs: What can go wrong?
4. Safety of Avandia:
5. Trials with no events
6. Graphical summary

## Acknowledgements:

- James Roger & Valerii Fedorov (RSU), for many discussions
- George Quartey (now at Roche) with whom I've developed a two-day course on meta-analysis

# 1. What is meta-analysis?

The statistical analysis of a large collection of analysis results from individual studies for the purpose of integrating the findings.

(Glass, 1978)

# History

- Fisher (1940s) started the ball rolling
  - Agricultural trials
  - Combining p-values



- Cochran (1950s) laid down the basics:
  - Inverse-variance weighting
  - Testing homogeneity



- Glass (1970s) coined the name
  - Showed efficacy of psychotherapy

# Early use in Medicine

- Yusuf et al (1985) used a meta-analysis to show that long-term beta-blockade following discharge from the coronary care unit after MI reduced mortality
- The Early Breast Cancer Trialists' Collaborative group (1988) showed that tamoxifen reduced mortality in women over 50 with early breast cancer

# Cochrane collaboration

- Started in 1993
- Towards evidence-based medicine
- Over 4,000 systematic reviews
  - Available on-line:  
<http://www.cochrane.org/>
  - Produced by volunteer healthcare professionals, overseen by editorial teams
  - Most systematic reviews include a meta-analysis (term usually used to refer to the phase of combining results)



# What data?

- Individual patient data
  - Available for in-house meta-analysis
  - Allows analysis of covariates
  - Methodology as for multi-centre trials
- Summary data
  - Use estimate and s.e. from each study
  - Range of special methods

## 2. How does it work?

- Summary data: “inverse variance” method is commonest
  - Statistic (e.g. treatment difference) from each study
  - Standard error of each statistic
- Weight each estimate by inverse variance
  - i.e.  $1/s.e.^2$
  - Imprecise studies make less contribution
  - Studies contribute in proportion to the number of patients (if variability is the same)
  - Studies contribute in inverse proportion to the variability (if number of patients is the same)

# Heterogeneity

- Inverse-variance method provides a combined estimate and a standard error
  - confidence intervals and a p-value can be derived
- Heterogeneity of the estimates can be calculated
  - heterogeneity is central in the interpretation
  - used to help decide whether the studies should all be combined
- **Clinical heterogeneity is at least as important as statistical heterogeneity**

# Example: dentifrices

Study	N1	Mean1	SD1	N2	Mean2	SD2
1	134	5.96	4.24	113	6.82	4.72
2	175	4.74	4.64	151	5.07	5.38
3	137	2.04	2.59	140	2.51	3.22
4	184	2.70	2.32	179	3.20	2.46
5	174	6.09	4.86	169	5.81	5.14
6	754	4.72	5.33	736	4.76	5.29
7	209	10.10	8.10	209	10.90	7.90
8	1151	2.82	3.05	1122	3.01	3.32
9	679	3.88	4.85	673	4.37	5.37

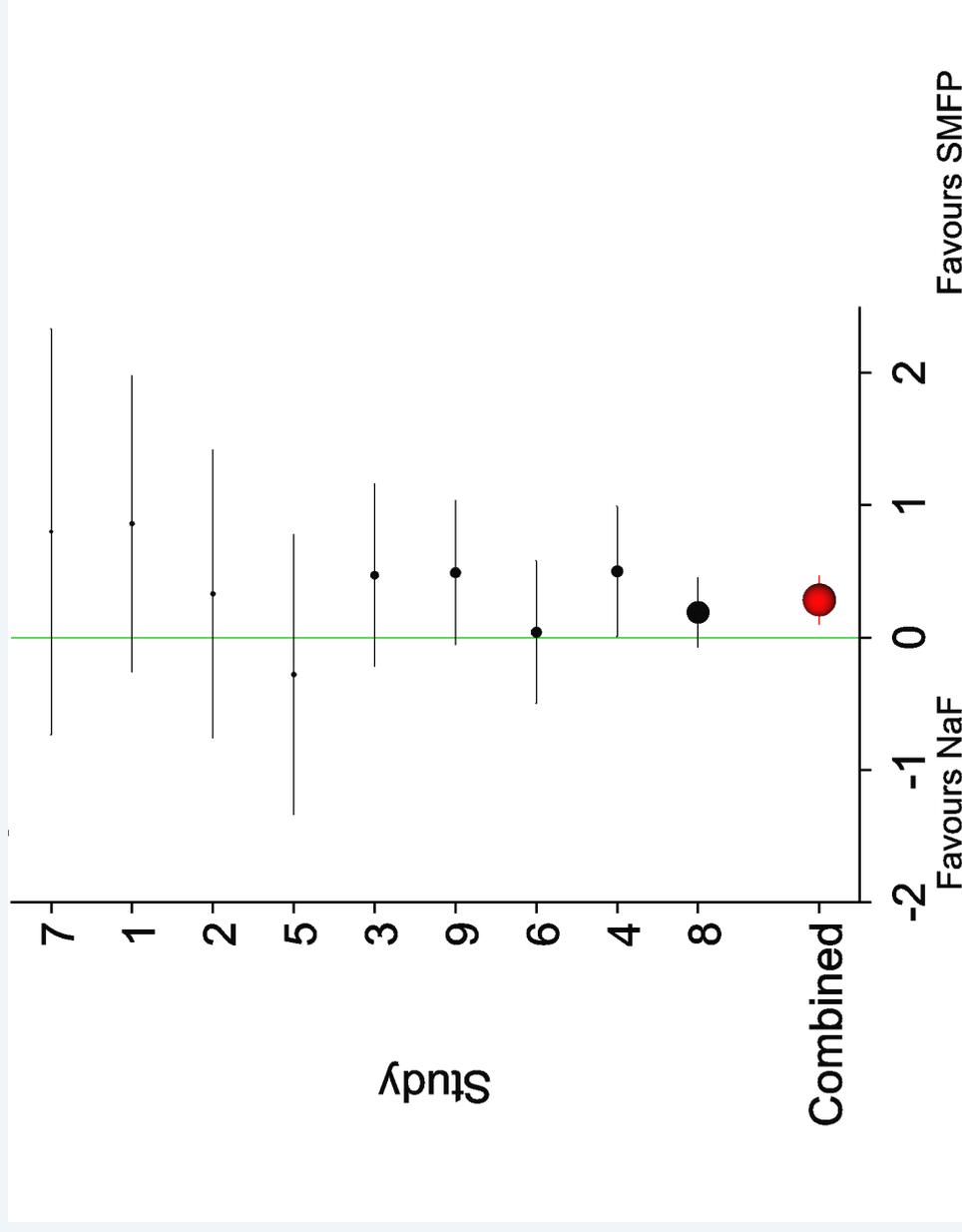
# Weights

- SEs can then be calculated

$$SE = SD \cdot \sqrt{\{1/N_1 + 1/N_2\}}$$

Study	Diff	SE	Weight	$w = 1/SE^2$
1	0.86	0.57	3	
2	0.33	0.55	3	
3	0.47	0.35	8	
4	0.50	0.25	16	
5	-0.28	0.54	3	
6	0.04	0.28	13	
7	0.80	0.78	2	
8	0.19	0.13	56	
9	0.49	0.28	13	

# Forest plot of NaF vs SMFP



Treatment diff. (SMFP - NaF) and 95% CI (DMFS units)

# Random effects

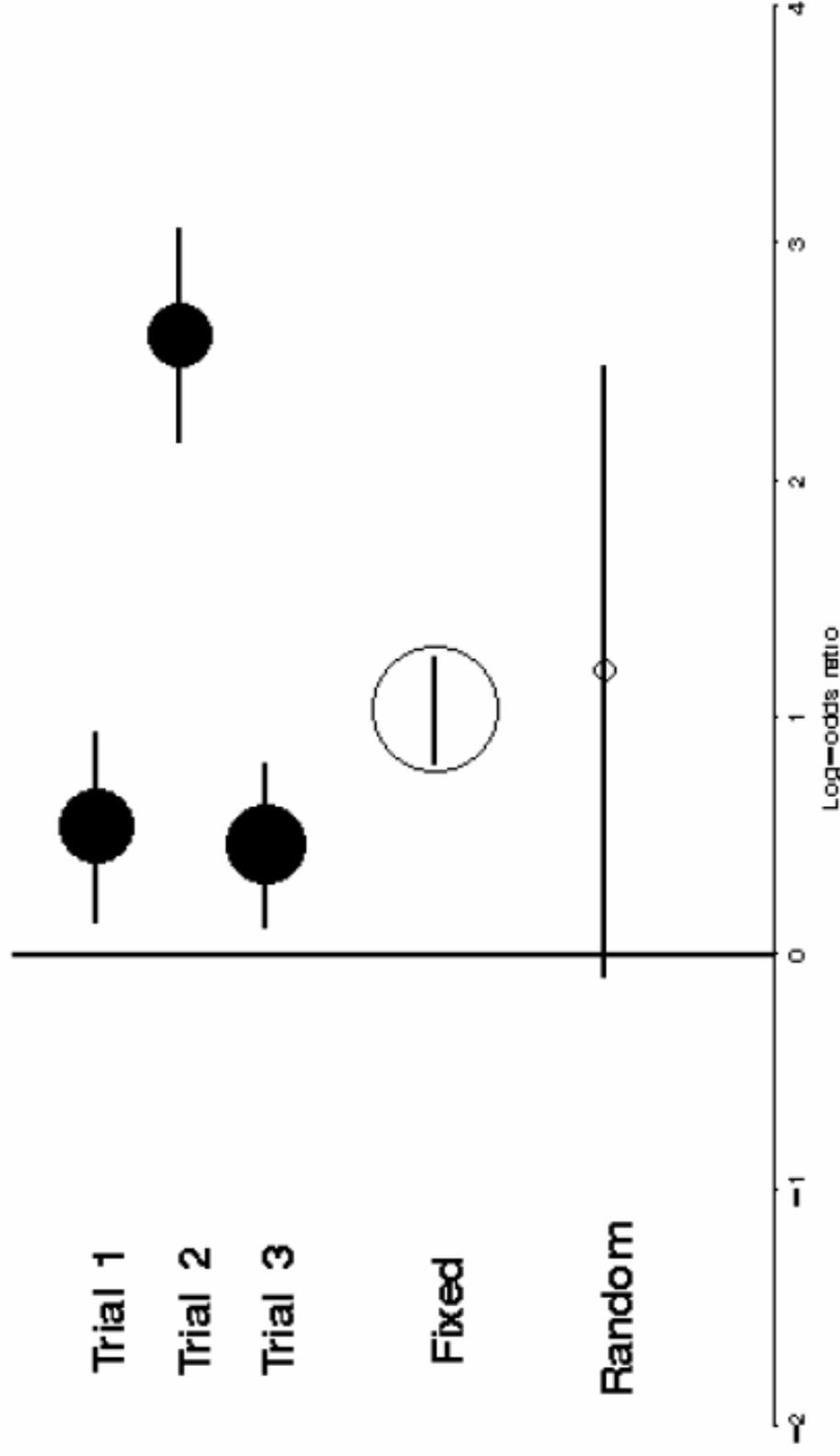
- Fixed-effects method assumes same difference in all studies
- Random-effects method assumes a distribution
  - Add between-study variance to the model
- DerSimonian-Laird method adjusts inverse-variance formula:
  - $Q = \sum w(d-d^*)^2$  where  $d$  is diff.,  $d^*$  is combined diff.
  - $\tau^2 = (Q - (k-1)) / (\sum w - \sum w^2 / \sum w)$  or 0 (if negative)
  - $w^* = 1 / (SE^2 + \tau^2)$
- Cochran  $Q$  used as indicator of heterogeneity
  - Or  $I^2 = 100(Q - (k-1)) / Q$  or 0 (if negative)

# Dentifrice heterogeneity

- $Q = 5.4$  ( $\chi^2$ -statistic with  $df=8$  if no heterogeneity)
- $T^2 = 0$
- $I^2 = 0$
- So the random-effects estimate is identical to the fixed-effect estimate

# But what if we get this?

Log-odds ratio of success (new treatment vs placebo)

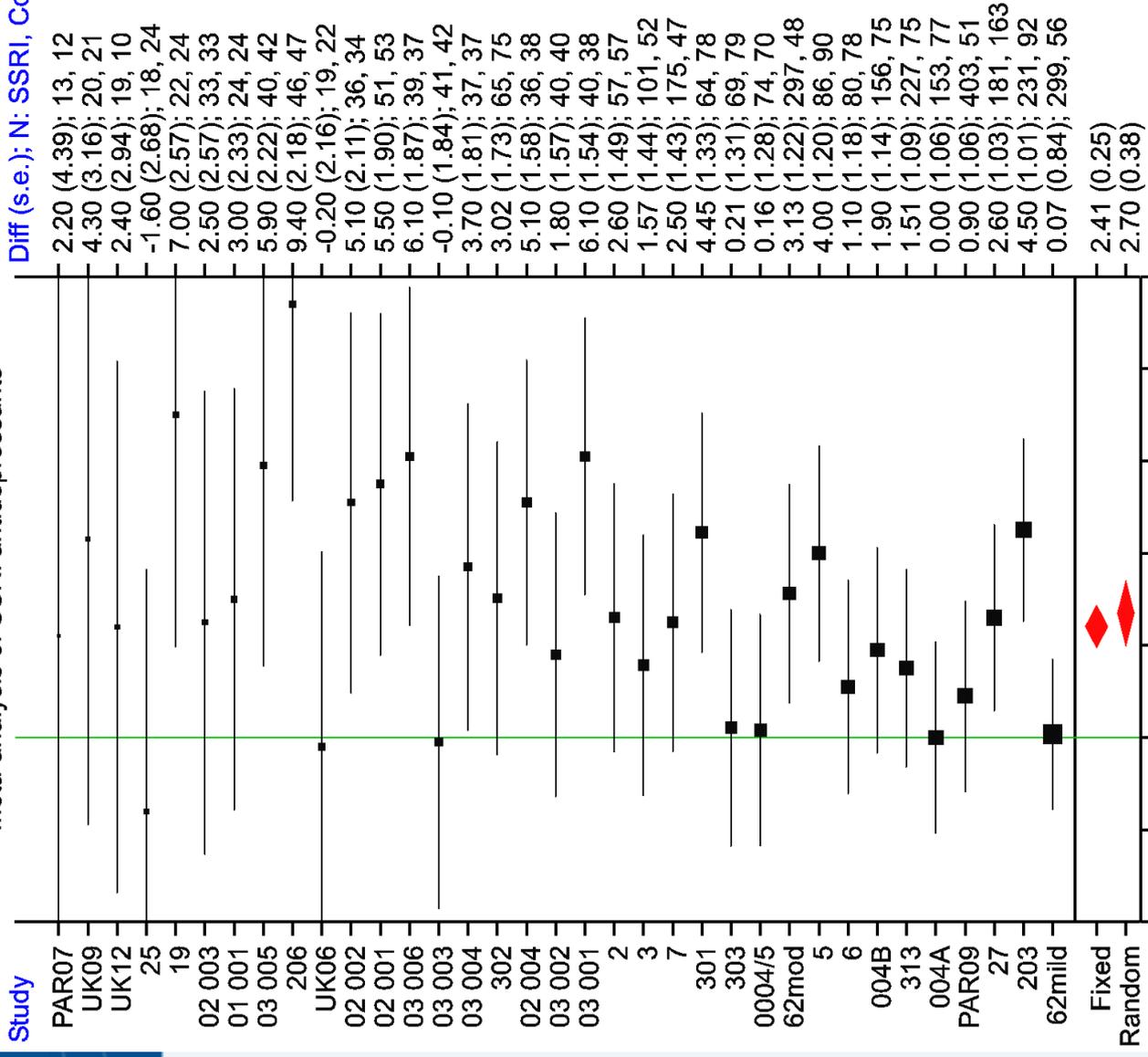


## 3. Efficacy of SSRIs

- Kirsch et al (PLoS Medicine, Feb 2008, and in Significance, 2008 Issue 2)
  - RCTs using SSRIs, assessing Hamilton depression scale
  - All trials provided in response to request to FDA
  - Paroxetine, fluoxetine, venlafaxine, nefazodone
  - 35 trials: 16 of paroxetine (cf. 352 trials on GSK's register!)
- Used naïve pooled summary, and naïve regression
  - No adjustment for imbalance of treatment arms
- Used naïve regression to investigate heterogeneity
  - Regressed mean change (from unpaired treatment arms) on baseline severity

Meta-analysis of SSRI antidepressants

Diff (s.e.); N: SSRI, Cont



Treatment diff. (SSRI - Placebo) and 95% CI (HAMD units)

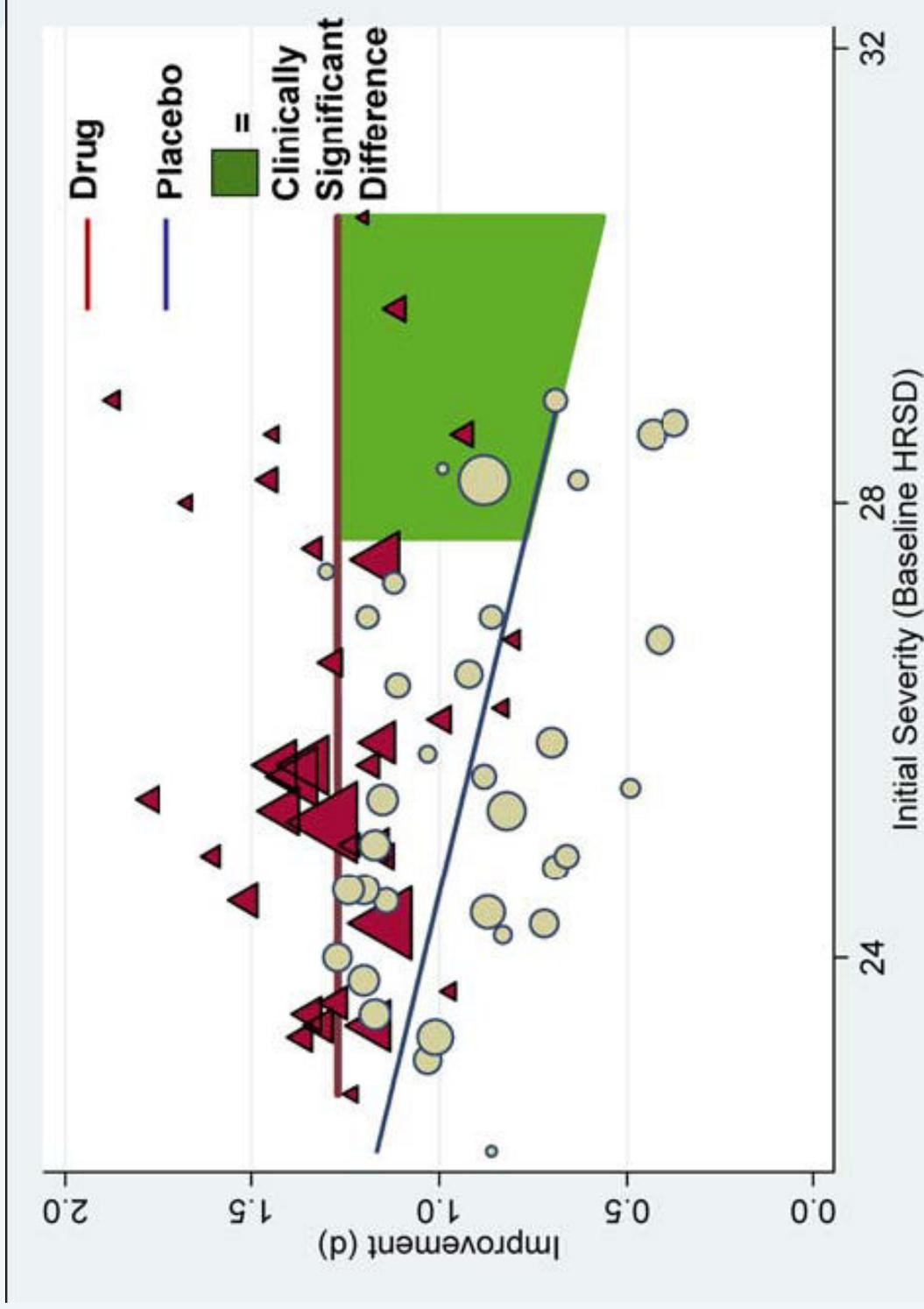
Favours Control Favours SSRI

# Combined estimate

- Naïve combined estimate: 1.80 units
- Fixed-effect method: 2.41 (s.e. 0.25)
- Random-effect method: 2.70 (s.e. 0.38)
- Significant heterogeneity ( $Q = 71.2$ ,  $df=34$ ;  $I^2 = 53\%$ )

<i>Drug</i>	<i>Ntrial</i>	<i>Fixed</i>	<i>Random</i>
Fluoxetine	5	1.65 (0.55)	2.06 (1.07)
Nefazodone	8	1.63 (0.44)	1.65 (0.49)
Paroxetine	16	3.22 (0.47)	3.38 (0.61)
Venlafaxine	6	3.23 (0.53)	3.54 (1.06)

# Regression analysis



## 4. Safety of Avandia

- Nissen & Wolski (2007)
  - RCTs using rosiglitazone, assess MI and CV death
  - Phase II to IV,  $\geq 24$  weeks, randomized comparator
  - 48 trials: six not detailed because there were no events
  - All 42 on the GSK Register, plus six candidates for those omitted
- Used the Peto method
  - Reasonable for rare events when effect is not large
  - Side-steps problems with trials that have events in only one arm (10 trials have no events, 20 have none under one treatment → only 18 trials with events in both groups)
  - Poor behaviour when highly unbalanced (8:1 or more) (Refs 3 & 5)
  - Biased estimates when the effect is substantial
  - Simulation with this set shows that the combined estimate has little bias and the properties of the significance test are satisfactory

# 48 trials

Study	Rosiglitazone		Comparator		Duration (weeks)
	N	MI	N	MI	
011	357	2	176	0	24
020	391	2	207	1	52
...					
dream	2635	15	2634	9	156
adopt	1456	27	2895	41	208
282	70	0	75	0	24
369	25	0	24	0	26
096	232	0	115	0	26
044	101	0	51	0	26
325	196	0	195	0	24
004	676	0	225	0	24

# Controversial issues

1. Trials not designed to study CV problems:
  - Identification of events not planned and recorded as carefully as in studies designed for this purpose
2. Comparator groups vary widely:
  - Placebo, Metformin, Sulfonylurea, Insulin
3. Rosiglitazone as monotherapy or as adjunct therapy
4. Populations vary widely:
  - Mild diabetics, insulin-treated diabetics, psoriasis patients
5. Different doses of rosiglitazone: 2mg to 8mg
6. Duration of treatment varies widely: 24 to 208 weeks
7. Events were rare:
  - Less than 2% pa in all but five treatment groups
  - No incidence at all in nearly half the treatment groups

**All of these cast doubt on the results and possible interpretation of the following meta-analyses**

# Naiïve analysis

- Looking at the pooled results gives the impression that there is no treatment effect at all:
  - 0.56% incidence of MI under Comp and 0.51% under Rosi (i.e. about 5 patients per 1000 in the trials had a heart attack on average)
- This ignores the treatment imbalance (Simpson's Paradox)
  - ADOPT trial was large, 2:1 randomization (Comp:Rosi), and a higher incidence rate (four-year study)
  - Naturally more MIs reported under Comp in this trial, and the Treatment effect is confounded with the variation in overall incidence
- **Moral: beware of pooling information without stratifying by Study**

# Scale of analysis

- **Analysing risk difference has problems:**
  - Risks are very likely to be related to duration
  - Scientifically, treatment likely to multiply risks rather than add to them
  - Wide range of incidence: 0.06% in Study 330 (psoriasis) to 3.1% in Study 211 (diabetics with CHF)
- **Analysing relative risks has problems:**
  - No information from 30 trials, if use log scale
  - But handles duration and is multiplicative
- **Odds ratio very similar to relative risk**
  - One-step method (Peto) excludes only 0-0 trials

# Risk difference

- Inverse-variance method (excluding 0-0 trials):
  - 0.18% greater risk on Rosi, i.e. 2 per 1,000, NNH=556
  - 95% CI [0.07%, 0.28%],  $p=0.001$
  - Weights: 40% '330', 9% Dream, 2% Adopt, 0% '0-0'  
0-0 trials would have infinite weight
  - Psoriasis trial 330 has nearly half the weight
- Add 0.5 correction factor for trials with a zero
  - 0.02% [-0.12, 0.17]  $p=0.74$
  - Weights: 13% '330', 17% Dream, 3% Adopt, 22% '0-0'
- Estimate depends entirely on chosen factor

# Mantel-Haenszel method

- Originally developed for odds ratio, but extended for relative risk and risk difference
  - Recommended method by Cochrane Collaboration
- Study weight is  $n_1 n_2 / N$ 
  - $n_i$  is no. of patients with Treatment  $i$ ,  $N = n_1 + n_2$
  - So weight depends only on size of trial
- Mantel-Haenszel estimate:
  - 0.19% [0.01%, 0.36%],  $p=0.034$
  - Weights: 4% '330', 20% Dream, 14% Adopt, 12% '0-0'
  - Fortuitously close to the IV method without 0-0 trials, despite very different weighting

# Adjust for duration

- Adjusting for duration of trial:
  - Risk range is unchanged (330 and 211 both 1-year), so still have problem of underlying model
  - Interpretation is improved in terms of exposure to drug
- Inverse-variance:
  - 0.10% pa, [0.02%,0.18%],  $p=0.016$
  - Weights: 24% '330', 46% Dream, 16% Adopt, 0% '0-0'
- Mantel-Haenszel:
  - 0.12% pa, [0.01%,0.23%],  $p=0.034$
  - Weights: 3% '330', 36% Dream, 35% Adopt, 5% '0-0'

# Random-effects

- The  $Q$  statistic is less than its expected value, and  $I^2 = 0$ 
  - Hence the random-effects approach gives the same result

# Odds ratio

There are several possible approaches using OR:

- (Inverse variance of log OR excludes 30 trials)
- Logistic reg.    1.427 [1.030, 1.977]     $p=0.0327$
- Scoring            1.429 [1.031, 1.980]     $p=0.0320$
- Conditional      1.426 [1.029, 1.975]     $p=0.0328$   
(Exact using mid-P)     $p=0.0339$
- Peto                1.428 [1.031, 1.979]     $p=0.0321$
- (Mantel-Haenszel excludes 30 trials)

# Bayesian approach

- Generalized linear mixed model
  - random Study effect
- Use “non-informative” priors
  - $N(0; 10,000)$  for mean (on log-odds scale)
  - $N(0; 10,000)$  for all Study effects (ditto)
- Fixed-effect for treatment
  - 0-0 trials don't contribute
  - 1.45 with 95% credible interval [1.03, 1.98]

**Method is unimportant (as long as it is appropriate)**

**The choice of data drives the results**

## 5. Trials with no events

- Agreement is reassuring, but 10 trials do not contribute
- Intuitively, they say something about relative risk and odds ratio:
  - An equal number of events (i.e. none) were observed
- But this intuition is based on prior expectation:
  - We expect that the risk is not actually zero, and that therefore there is an underlying relative risk
  - Without prior information, **there is NO information about relative risk or odds ratio**, because the observed risks are zero

# Trials with no events (cont.)

There are three ways to address this problem

- **Bayesian approach**
  - Need priors, and different people (e.g. pharma companies and regulators) will naturally not agree
- **“Continuity correction”**
  - Adjust the zeroes slightly, on the grounds that they are expected to be non-zero
  - Introduces deliberate bias
- **Combine trials to reduce sparsity**
  - Danger of confounding and Simpson’s Paradox
  - Standard approach for sparse contingency tables

# Bayesian approach

- Random-effects model:
  - 0-0 trials contribute to the results
  - “non-informative”  $U(0; 10)$  for SD ( $\tau$ )
  - Other priors as for Bayesian fixed-effects model
  - 1.52 [0.97, 2.36]
- So 0-0 trials increase the estimate a little, but the credible interval also widens
  - Surprising that they increase the estimate
  - I don't know why

# Adjusting the zeroes

- Add a small number to trials with zero events, to trials with zero in at least one arm, or to all the trials regardless
- Some software does this automatically, using the value 0.5
- Research indicated that this produces less biased results than ignoring the zero results (Refs 2 & 6)
  - However, they looked at risks no smaller than 10%
  - Here it is <1%; the 0.5s tends to swamp any real effects (Ref 7)
- E.g., adjust both counts in trials where one or both is zero
  - 0.5 reduces the combined estimate to 1.29 [0.95, 1.74]  $p=0.10$
  - 0.1 to reduce swamping gives 1.40 [1.02, 1.93]  $p=0.040$
  - 0.01 returns us almost to the result omitting the zero trials
- “Treatment-arm” correction, using  $1/N$  from other treatment arm (Ref 8): 1.43 [1.03, 1.98]  $p=0.033$

# Pooling discriminately

- Combine trials to avoid having no events
- Match trials by duration, treatment and rand. ratio

Trials with no MI events				Matched trials with some MI events			
Trial	Dur.	Treatments	Ratio	Trial	Dur.	Treatments	Ratio
095	26	Rosi+Ins vs Ins	2:1	082	26	Rosi+Ins vs Ins	2:1
234	26	Rosi+SU vs SU	2:1	079	26	Rosi±SU vs SU	2:1
331	52	Rosi vs Plac	2:1	330	52	Rosi vs Plac	3:1
009	24	Rosi+Met+Ins vs Ins	1:1	347	24	Rosi+Ins vs Ins	2:1
282	24	Rosi+Met vs SU+Met	1:1	284	24	Rosi+Met vs Met	1:1
369	26	Rosi vs SU	1:1	162	26	Rosi+SU vs SU	1:1
096	26	Rosi+SU vs SU	2:1	079	26	Rosi±SU vs SU	2:1
044	26	Rosi+Met vs Met	2:1	094	26	Rosi+Met vs Met	2:1
325	24	Rosi vs SU	1:1	143	24	Rosi+SU vs SU	1:1
004	24	Rosi±SU vs SU	3:1	132	24	Rosi+SU vs SU	4:1

# Pooling (cont.)

- Effect of including the extra trials is minimal
  - estimates become 1.433 (1.035, 1.985)  $p=0.0303$
- Surprising that this **increases** the estimate slightly
  - Non-intuitive (because of prior expectation)
  - Pooling reduces the underlying heterogeneity, and this increases the effect on the marginal scale
- Confirms that there is indeed no information about the odds ratio in these 10 trials (unless we adopt informative priors)

# Result

- There is a signal from the MA (not evident in any study alone) that there are slightly more MIs for patients in the trials who received rosigitazone
- Estimated odds ratio 1.43 (can also interpret as risk ratio)
- Could say that the rosigitazone patients experienced a 43% higher risk of MI:
  - But it is confusing to talk of % of risk, which is itself often a %
  - Also, a risk difference would be more relevant to patients
- **Do not analyse on risk scale to get risk difference:**
  - Use the model to predict the risk difference
  - E.g. mildly diabetic patient with risk of 0.5% p.a. → 0.7% p.a. on average (risk difference of 0.2% or two in a thousand)
  - However, **this average is over all comparators in this collection of trials**, whereas patient knows own regimen

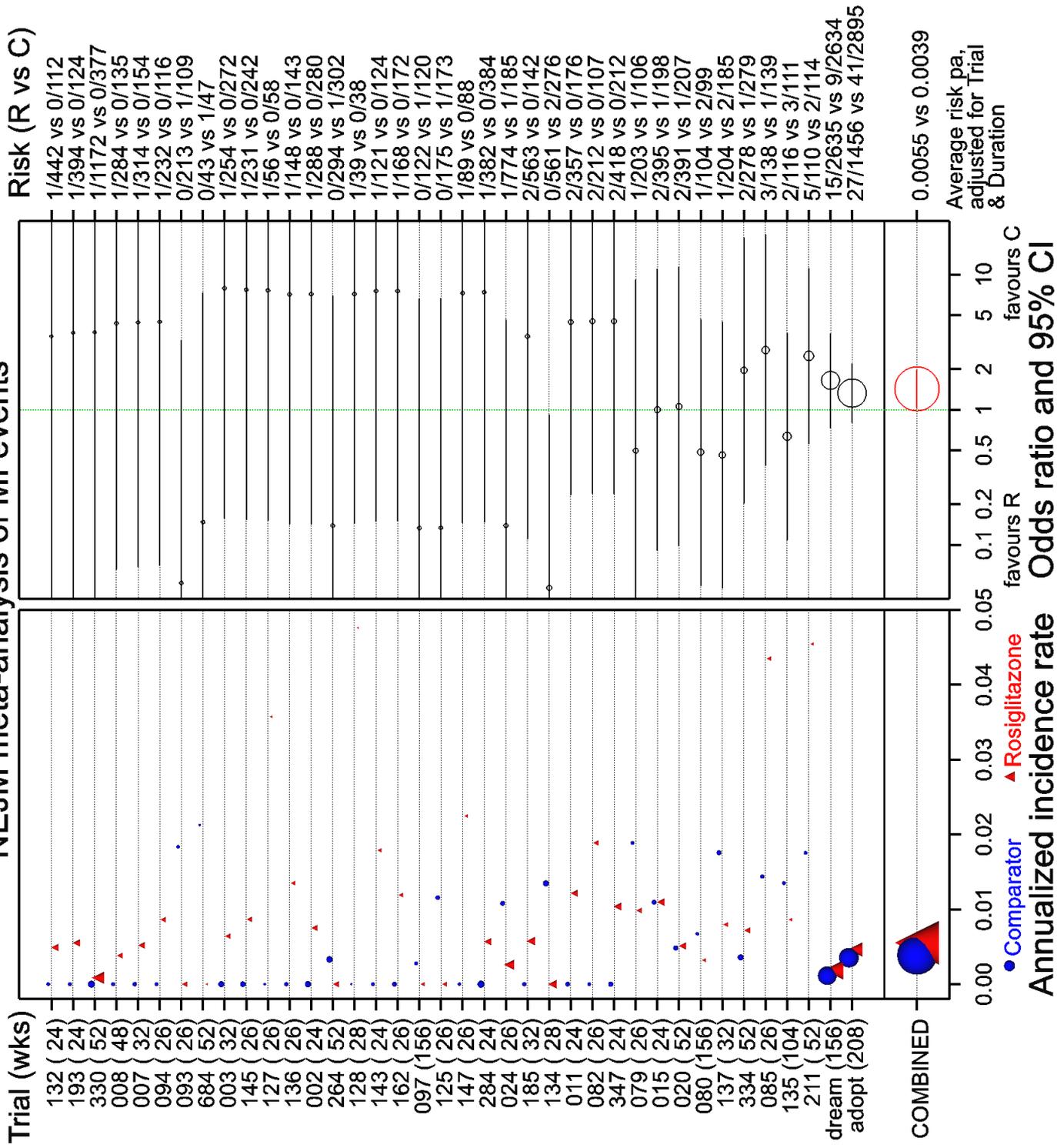
# Prediction

- Summary on the risk scale, averaging over the studies, adjusting for the differences
  - “Predicts” the average risk under adjusted conditions: equal numbers on each treatment
  - Stats calculated by LSMEANS /OM in the GLM procedure of SAS (not in GENMOD or LOGISTIC!)
- Fit logistic, adjusting for duration (offset), gives predicted average risk p.a. (from GenStat):
  - Comparator 0.34% (s.e. 0.050) Diff 0.14% (s.e. 0.066)
  - Rosiglitazone 0.48% (s.e. 0.059)
- It is important to average on the risk scale, not on the logistic scale (only option in SAS)

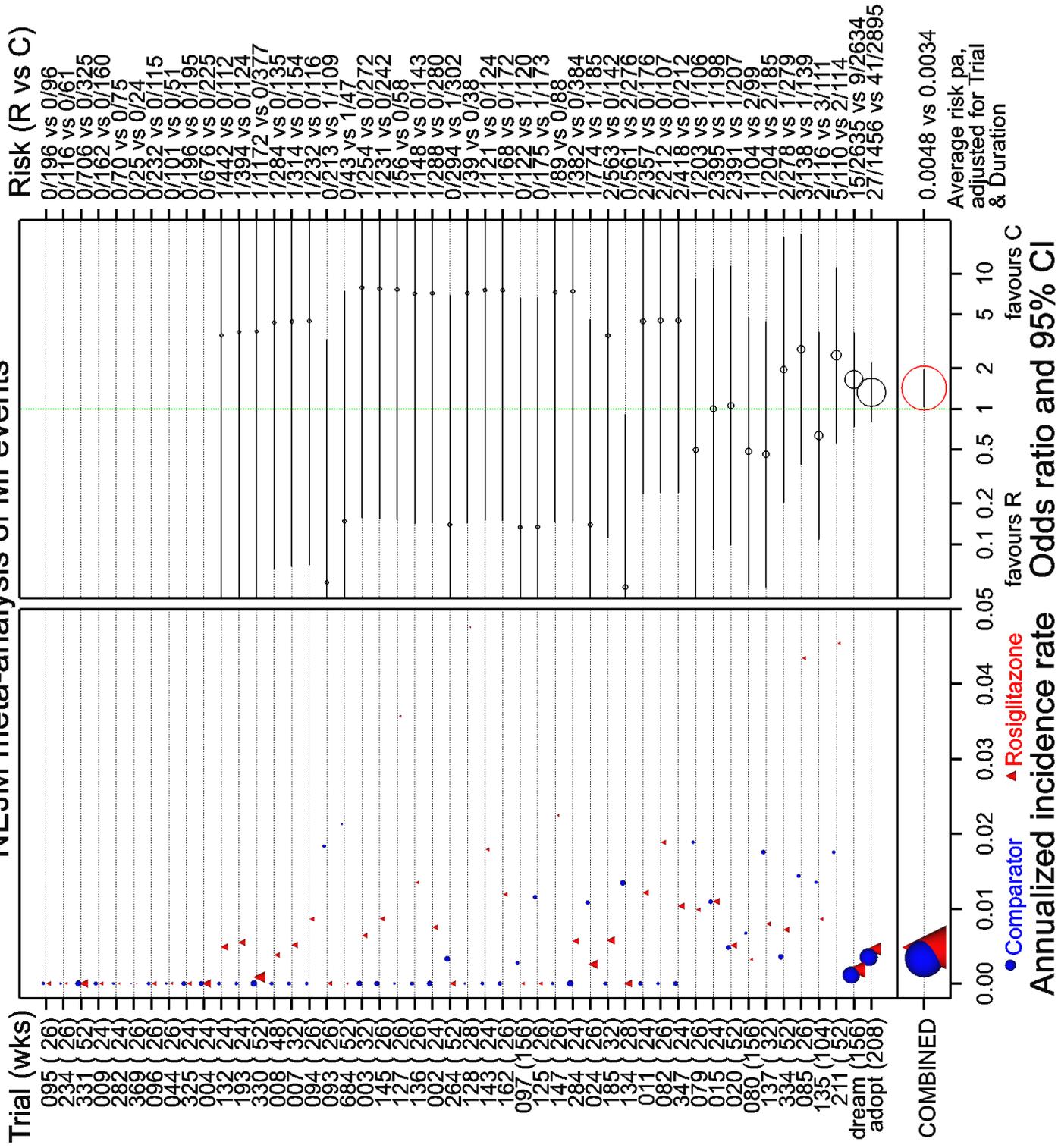
## 6. Graphical summary

- Graphical methods enhance interpretation
- Interval plot, or “Forest plot”, is standard for MA
  - Design to show weights of components
  - Add raw data to allow look-up
  - Give combined estimate(s) in margin
- Add panel of actual incidence, for context
- Add prediction as summary of combined effect

# NEJM meta-analysis of MI events



# NEJM meta-analysis of MI events



# Context

- GSK patient-level meta-analysis (to FDA in 2006)
  - Separate analyses for different comparators
  - Many of the same trials, but not ADOPT or DREAM
  - Indication of some marginally raised incident rates
- GSK-commissioned observational study (2006)
  - 33,000 patients on oral anti-diabetics
  - Composite CV endpoint (MI and revascularization)
  - Hazard ratio 0.93 for Rosi vs other treatments
- Recent paper by Dahabreh in *Clinical Trials* (Ref 1)
  - Added new results from large trial (RECORD), and updated event counts
  - 1.43 estimate reduced to 1.33 – 1.23 (dep. on method)

# References

1. Dahabreh IJ (2008). Meta-analysis of rare events: an update and sensitivity analysis of cardiovascular events in randomized trials of rosiglitazone. *Clinical Trials* **5**:116–120.
2. Gart JJ, Zweifel JR (1967). On the bias of various estimators of the logit and its variance with application to quantal assay. *Biometrika* **54**:181–187.
3. Greenland S, Salvan A (1990). Bias in the one-step method for pooling study results. *Statistics in Medicine* **9**:247–252.
4. Nissen SE, Wolski K (2007). Effect of rosiglitazone on the risk of myocardial infarction and death from cardiovascular causes. *New England Journal of Medicine* **2007**; 356.
5. Robbins J, Greenland S, Breslow N (1986). A general estimator for the variance of the Mantel-Haenszel odds ratio. *American Journal of Epidemiology* **124**:719–723.
6. Sankey SS, Weissfeld LA, Fine MJ, Kapoor W (1996). An assessment of the use of the continuity correction for sparse data in meta-analysis. *Communications in Statistics – Simulation and Computation* **25**:1031–1056.
7. Sutton AJ, Cooper NJ, Lambert PC, Jones DR, Abrams KR, Sweeting MJ (2002). Meta-analysis of rare and adverse event data. *Expert Review of Pharmacoeconomics and Outcomes Research* **2**:367–379.
8. Sweeting MJ, Sutton AJ, Lambert PC (2004). What to add to nothing? Use and avoidance of continuity corrections in meta-analysis of sparse data. *Statistics in Medicine* **23**:1351–1375.